ABSTRACT
In this research the differential gears analyzed for vibration effect on whole system to optimize the life of the gears under different frequency in the platform of Ansys-14.0 with help of solid work modelling. In this analysis the gear housing also affected by vibration in casing that surrounds the gear box. The function of gear is to protect and provide a platform for gear transmission. It also provides supports for moving parts and protection from outside environmental condition. The differential couples, the propeller shaft to the pinion, which in turn runs on the ring gear of the differential & it also helps as reduction gearing. Hence will get subjected to vibration so it becomes necessary to evaluate the response of differential gear housing in such vibrations and also to find out there natural frequencies. This can be an important tool while designing the differential gear housing free from fatigue failures caused by the resonance. The design of the gear housing should incorporate a methodology for dealing with factors causing vibrations and to promote scientific means to minimize the effects of frequencies. This vibration analysis is done by using Ansys 14.0 software as a computational technique and validation.

KEYWORDS: differential gears, natural frequency, Ansys 14.0.

I. INTRODUCTION
In automobiles and other wheeled vehicles, the differential permit each of the driving wheels to rotate at different speeds, while for most vehicles supplying equal torque to each of them. A vehicle's wheels rotate at divergent speeds, mainly when turning corners. The differential is designed to operate a pair of wheels with same torque while permit them to rotate at different speeds. In vehicles without a differential, such as karts, both driving wheels are forced to rotate at the equal speed, generally a common axle driven by a simple chaindrive mechanism. When cornering, the inner wheel needs to travel a shorter distance than the outer wheel, so with no differential, the result is the inner wheel spinning and/or the outer wheel dragging, and this results in difficult and unpredictable handling, damage to tires and roads, and strain on the entire drive train. The Differential transmits mechanical energy from a prime mover to an output device. It also vary the speed, direction of mechanical energy. Differential gearbox is used when high speed, large power transmission where noise abatement is important. In this present work the analysis is conducted on the gearbox, to verify the natural frequency For this purpose the modelling of the transmitting power gear assembly on solidwork were made and fem based structural behaviour were carried out on the ansys 14.0 analysis tool.

II. RESEARCH WORK
➢ To design a gear box housing under the plateform of solodwork.
➢ To findout the natural frequency of gearbox under different condition through ansys 14.0.

III. ANALYSIS WORK
The project is divided into two domains:
1. Modal Analysis
2. Stress analysis

Modal Analysis: The natural frequencies of in free conditions are calculated using Ansys14.0 and by the application of boundary conditions to compare with experimental and operating frequencies.
Stress Analysis: It is static analysis of the model by applying boundary conditions and forces which are calculated according to the data provided by the instructor.

1.1 Model analysis Modal analysis is a term used to describe any of the processes employed to extract a structure’s modal properties (natural frequencies, modal damping factors, and mode shapes) from information about the structure that is presented in a different format. When these properties are extracted from a theoretical analysis of the dynamic behavior.

1.2 Gear mesh frequency This is the frequency most commonly associated with gears and is equal to the number of teeth on the gear multiplied by the actual running speed of its shaft. A typical gearbox will have multiple gears and therefore multiple gear meshing frequencies. A normal gear mesh signature will have a low-amplitude gear mesh frequency with a series of symmetrical sidebands, spaced at the exact running speed of the shaft, on each side of the mesh components. The spacing and amplitude of these side bands will be exactly symmetrical if the gearbox is operating normally. Any deviation in the symmetry of the gear mesh signature is an indication of incipient gear problems. Fig. 2 shows a diagram of a basic test system configuration.

The gear mesh frequency is considered for following conditions:
1. Idling
2. Cruising
3. Maximum speed

Gear mesh frequency \( F = k \frac{N}{60} \) Hz Where, \( k \) = number of teeth on gear \( N \) = speed of the rotating shaft (on which gear was mounted)

IV. CALCULATIONS OF A CROWN GEAR AND PINION

The main aim of the project is to verify the best material for the gears in the gearbox at higher speeds by analyzing stress, displacement and also by considering weight reduction focus on the mechanical design and contact analysis on assembly of gears in the gearbox when they transmit power at different speeds at 2400 rpm, 5000 rpm and 6400 rpm. Analysis is also conducted by varying the frequencies. Differential gear is modeled in Solidwork. The ANSYS 14.0 fem software were used as the analysis tool for determining the structural behavior of various composites under the given loading conditions.

Specifications of Used Heavy Vehicle

Assumptions:
- Gear profile: -20 degree full depth involute profile (standard)
- Pressure angle (\( \alpha \)) :-20 degree
- Bevel gear arrangement = 90 degree
- Pitch cone Angle (\( \phi \)) = 45
- Back cone Angle (\( \beta \)) = 45
- Module (\( M \)) = 10
- Number of teeth on gear = \( Z_g \) = 50
- Number of teeth on pinion = \( Z_p \) = 8

Velocity Ratio (V.R)
\[
V.R = \frac{\text{T.G}}{\text{T.P}} = \frac{\text{D.G}}{\text{D.P}} = \frac{\text{N.P}}{\text{N.G}}
\]
\[
V.R = \frac{50}{8} = 6.25
\]
\[
V.R = \frac{2400}{NG}
\]
\[
NG = 384 \text{rpm}
\]

Minimum no. of teeth on pinion (\( Z_p \))

For satisfactory operation of bevel gears the number of teeth in the pinion must not be less than hence the assumed value of the pinion is in safe condition

Pitch circle diameter (\( D \))

Pitch circle diameter for the gear (\( D_g \)) = \( M \times Z_g \)

Pitch circle diameter for the pinion (\( D_p \)) = \( M \times Z_p \)

Pitch angle (\( \theta \))

Since the shafts are at the right angles, the pitch
angle were given as:
For the pinion = \( \theta_p = \tan^{-1}(1/v.r) \)
Pitch angle of gear \( \theta_g = 90^\circ - 9 = 81^\circ \) 
formative number of teeth (Te)
for the pinion \( Z_{ep} = Z_p \sec \theta_p = 8 \sec 9 = 8 \)
for the gear \( Z_{eg} = Z_g \sec \theta_g = 50 \sec 81 = 319.622 \)

1. Pitch Cone Distance (AO):
   \[ AO = \sqrt{\left(\frac{d_1}{2}\right)^2 + \left(\frac{d_2}{2}\right)^2} \]
   \[ AO = 250\text{mm} \]

2. Face width (b)
   \[ b = \frac{AO}{3} \]
   or \[ b = 10 \]

V. CALCULATION OF GEAR AND PINION

1. Pitch circle diameter (D)
   Diameter of sungear = \( D_g = 150\text{mm} \)
   Diameter of pinion = \( D_p = 70\text{mm} \)

2. Number of tooth on gear
   Number of teeth on gear = \( Z_g = 18 \)
   Number of teeth on pinion = \( Z_p = 15 \)
   \[ D = D_g + D_p = 220 \]
   \[ T = Z_g + Z_p = 33 \]

3. Module = \( M = \frac{D}{T} = 220/33 = 6.66 = 7 \) (according to stds)

4. Velocity Ratio
   \[ V.R = \frac{Z_g}{Z_p} = \frac{D_g}{D_p} = \frac{NP}{NG} \]
   \[ V.R = \frac{150}{70} = 2.142 \]
   \[ V.R = NP/NG = 2.142 = 2400/NG \]
   \[ NG = 1120.448\text{rpm} \]

5. Pitch angle
   Since the shafts are at right angles therefore pitch angle
   for the pinion = \( \theta_p = \tan^{-1}(1/v.r) \)
   \[ = \tan^{-1}(1/2.142) = 25.025 \]
   Pitch angle of gear \( \theta_g = 90^\circ - 25.025 = 64.974 \)

6. Formative Number Of Teeth
   For the pinion = \( Z_{ep} = Z_p \sec \theta_p = 15 \sec 25.025 = 16.554 \)
   For the gear = \( Z_{eg} = Z_g \sec \theta_g = 8 \sec 64.974 = 42.55 \)

7. Pitch Cone Distance (AO):
   \[ AO = \sqrt{\left(\frac{d_1}{2}\right)^2 + \left(\frac{d_2}{2}\right)^2} \]
   \[ AO = 82.7\text{mm} \]

8. Face Width (b): \( 82.7/3 = 27.5 \text{ mm} \)

VI. FEM ANALYSIS OF THE GEAR

FEM, A computer based analysis technique for calculating the strength and behaviour of model during the given limits. In the FEM the model is represented as finite elements and are joined at special points which are called as nodes. Finite element analysis is the numerical solution of the mechanical components that are acquired by
discretizing the mechanical elements into a small finite number of building blocks (known as elements) and by investigation those mechanical components for their acceptability and reliability. FEM is the simple technique as compared as the theoretical methods to discover the stress developed in a pair of gears. Models for numerical analysis have been prepared in SOLIDWORK and these have been bring in into ANSYS as IGES files for further analysis. The proportions of gear obtained from theoretical analysis have been used for preparing geometric model of gear. The condition for analysis has been assumed as static.

VII. MESHING OF GEAR ASSEMBLY
In the analysis of the gear assembly it is mandatory to study of its structural behaviour at different load and condition. 3-D model of the gear assembly were made in solidwork and were carriedout in ansys analysis software as an iges file format. thereafter importing the model in ansys the suitable material was applied to the model and then meshing were done in ansys by which the whole body is devided into small tethydral element connected by nodes. the tottal node and element for the two were given in t

![Solid model of differential gear box in ansys 14.0](image)

**Mesh model**
Coarse meshing along with the refined meshing on joints is done to get accurate results.

![Coarse meshing and refined meshing](image)

**Problem formulation**
A natural frequency, epitomize by resonance is the characteristics of the part or subassemblies of a required product. This becomes notable while assess performances of applications where human comfort of the component life has a prominence on the function. Automobiles for example, are subjected to vibrations in terms of caused by the engine. The components making up the subassemblies need to be evaluated for this phenomenon. The design of the component should incorporate a mode for dealing with factors causing undesirable levels of vibration or to support any scientific means of problem solving that would decrease the harmful effects of resonance.
Result

After analysis of all the stresses and formulation the following natural frequencies are obtained.
VIII. CONCLUSION
After analysis of the differential gear assembly the natural frequencies on different modes it has been obtained which are as under :-
IX. REFERENCES


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